

**Semester One Examination 2011**

**Question/answer booklet**

**YEAR 12 MATHEMATICS**

**3C/DMAT**

**Section One**

**(Calculator-Free)**

|  |
| --- |
| Student Name: **\_\_\_\_\_\_\_\_\_SOLUTIONS\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_** |

Circle your teacher’s name

S. ROWDEN N. EDMUNDS

**Time allowed for this section**

Reading time before commencing work: 5 minutes

Working time for section: 50 minutes

**Material required/recommended for this section**

**To be provided by the supervisor**

Question/answer booklet for Section One

Formula sheet

**To be provided by the candidate**

Standard items: pens, pencils, pencil sharpener, highlighter, eraser, ruler

Special items: nil

**Important note to candidates**

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

**Structure of this examination**

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | Number of questions available | Number of questions to be attempted | Suggested working time (minutes) | Marks available |
| **Section One:**  **Calculator-free** | **10** | **10** | **50 minutes** | **40** |
| Section Two:  Calculator-assumed | 15 | 15 | 100 minutes | 80 |
| Total marks | | | | 120 |

**Instructions to candidates**

1. Answer the questions in the spaces provided.
2. Spare answer pages are provided at the end of this booklet. If you need to use them, indicate in the

original answer space where the answer is continued i.e. give the page number.

1. **Show all your working clearly.**

Your working should be in sufficient detail to allow your answers to be

checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks.

**For any question or part question worth more than two marks, valid working or justification is required to receive full marks.**

If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

1. It is recommended that you **do not use pencil** except in diagrams.

# Section One: Calculator-Free 40 Marks

This section has **Ten (10)** questions. Attempt **all** questions.

\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

**Question 1 (3 marks)**

Explain how you would find the area of the region bounded by the *x*-axis and the equations , *x* = -1 and *x* = 4. You are not required to find the area.



|  |
| --- |
| **Solution** |
| Find the definite integral over the boundary -1 to 4 of the absolute value of the function  Or  Find the opposite of the definite integral for the boundary -1 to 3 for function plus the definite integral for the boundary 3 to 4 for the function |
| **Specific behaviours** |
| ✓definite integral  ✓correct boundaries  ✓absolute value of function  Or  ✓ opposite of definite integral of the function between -1 to 3  ✓ definite integral of the function between 3 to 4  ✓ add two areas |

**Question 2 (5 marks)**

Differentiate the following: (do not simplify your answers)

(a) 

[1]

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓correct derivative |

(b) 

[2]

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓  ✓ |

(c) 

[2]

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓applies quotient rule correctly  ✓applies chain rule correctly |

**Question 3 (4 marks)**

In a probability experiment, events *M* and *N* are such that

 ,  and 

Find

(a) 

[2]

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ identifies  as the complement of  ✓ correct |

(b) 

[2]

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ determines  ✓ uses addition rule to correctly determine *P*(*N*) |

**Question 4 (7 marks)**

Determine the following integrals:

(a) 

[1]

|  |
| --- |
| **Solution** |
| If c is omitted from this question 0 marks |
| **Specific behaviours** |
| ✓correct answer |

(b) 

[2]

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓separates into expression with 2 terms  ✓ correct answer |

**Question 4 Continued**

(c) 

[2]

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓raise the power of the function by one  ✓divides by both raised power and derivative of 3*x* – 2 |

(d) 

[2]

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓✓applies chain rule |

**Question 5 (3 marks)**

Find the equation of the tangent to the curve at (-1, -1).

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓correct derivative  ✓correct gradient at given point  ✓determines correctly the y intercept and hence states equation |

**Question 6 (5 marks)**

Solve the system of equations



|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓✓reduces the system of equations to 2 equations with 2 variables  ✓reduces to 1 equation with 1 variable and solves equation  ✓✓back substitutes to find other 2 variables |

**Question 7 (3 marks)**

Determine the value of *b* for the following, given *b* is a positive integer.

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|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓integrates function  ✓substitutes upper and lower boundaries  ✓solves correctly for b |

**Question 8 (3 marks)**

Solve for *y* the inequality 

|  |
| --- |
| **Solution** |
| -1 < y < 1 |
| **Specific behaviours** |
| ✓simplifies inequality  ✓identifies critical values  ✓tests critical regions and states correct answer |

**Question 9 (2 marks)**

Find 

|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓correctly uses the Fundamental theorem of Calculus  ✓uses the chain rule |

**Question 10 (5 marks)**

Simplify the following:



|  |
| --- |
| **Solution** |
|  |
| **Specific behaviours** |
| ✓ correct factorisation for first fraction   correct factorisation for second fraction  ✓ invert second fraction and multiply  ✓ simplifies division correctly  ✓ states restrictions on division |

**Additional working space**

Question number: \_\_\_\_\_\_\_

**Additional working space**

Question number: \_\_\_\_\_\_\_

**Additional working space**

Question number: \_\_\_\_\_\_\_